

# Thermal vacancy thermodynamics and ordering kinetics in B2 AB intermetallics

COST 535, COST P19

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# Outline:

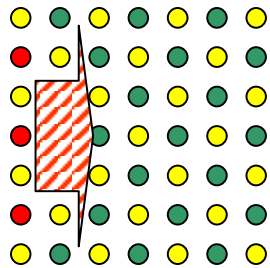
- „Order-order” kinetics
- NiAl – surprising experimental result
- MC simulations with temperature-dependent vacancy concentration
- Model for vacancy thermodynamics
- Results

# DIFFUSION

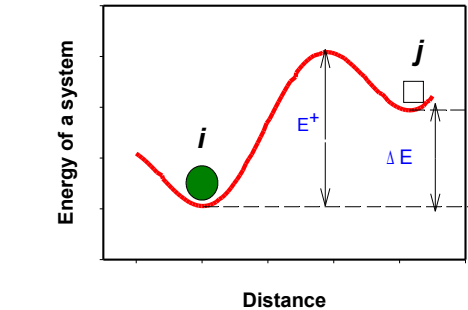
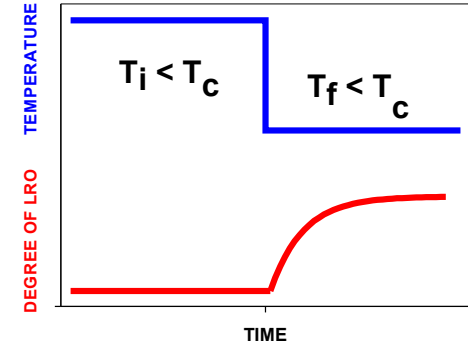
# AND

# „ORDER-ORDER” kinetics

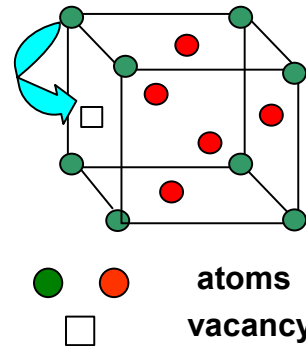
in intermetallics



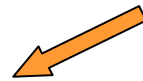
● A-atoms  
● B-atoms  
● A-tracer atoms



**COMMON ELEMENTARY MECHANISM:**  
**atomic jumps to vacancies**

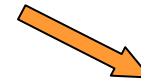


**SPECIFIC FEATURES: correlation of atomic jumps**



## DIFFUSION

Minimisation of the energetic cost of local LRO perturbation by jumping atoms:  
„six-jump-cycle”, ASB, triple defect mechanism, antisite diffusion etc.



## ORDER-ORDER kinetics

Formation of equilibrium atomic configuration:  
generation/elimination of antisite defects

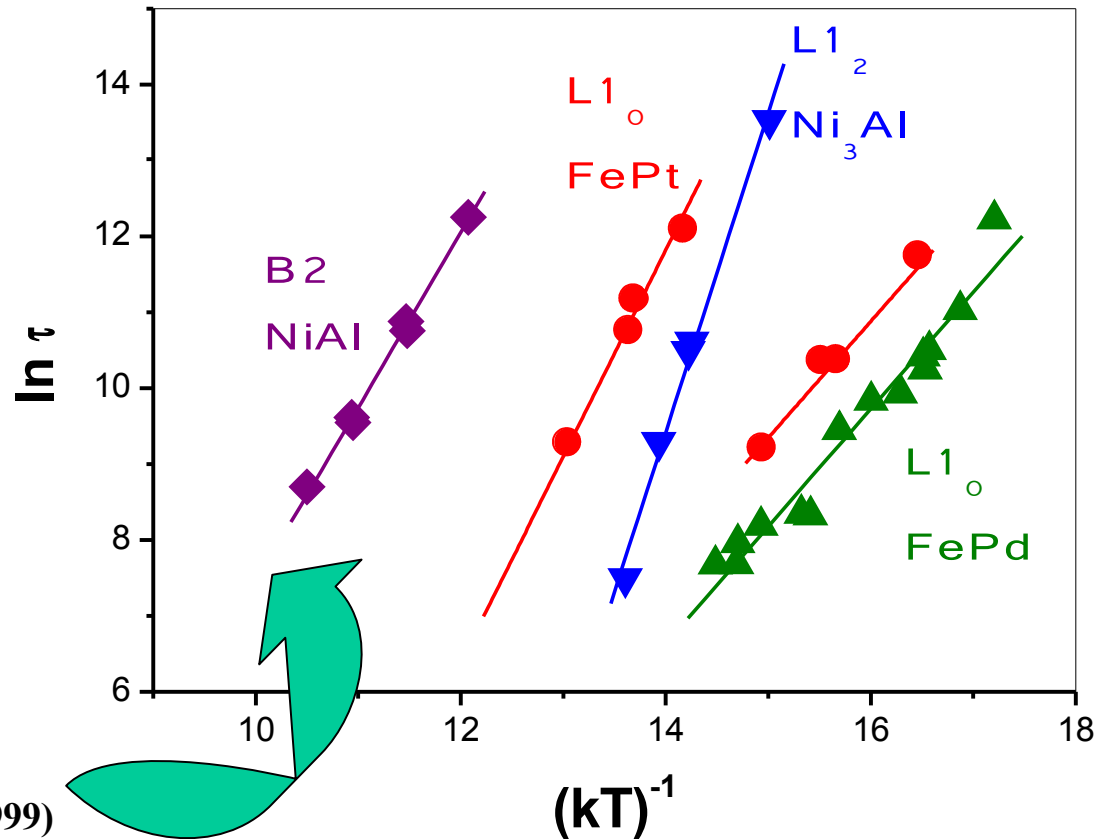
**CONCLUSION: BOTH METHODS YIELD COMPLEMENTARY INSIGHT INTO ATOMIC JUMP DYNAMICS**

# SYNTHESIS: analysis of „order-order” relaxation isotherms in **bulk** intermetallics

Process markedly slower than in  $\text{Ni}_3\text{Al}$  despite extremely high vacancy concentration:

$\text{Ni}_3\text{Al}$ :  $C_v=10^{-9}$  at  $T=T_m/2$

$\text{NiAl}$ :  $C_v=10^{-2}$  at  $T=T_m/2$

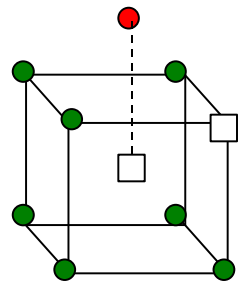


H.-E. Schaefer et al., *Intermetallics*; 7, 277, (1999)

R.Kozubski et al., *Intermetallics*, 11,897-905,(2003).

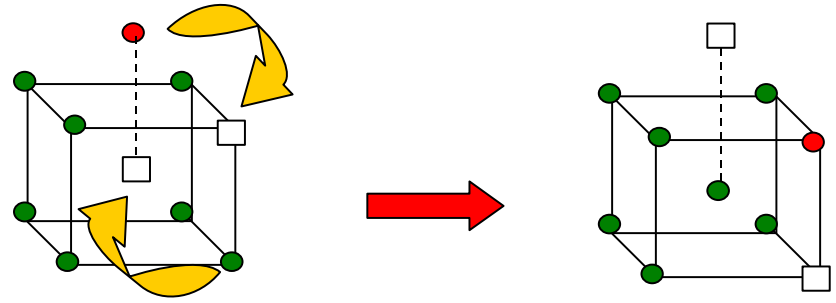
**GENERATION OF ANTISITE DEFECTS** without perturbing superlattice geometry:

Initial (starting) configuration:



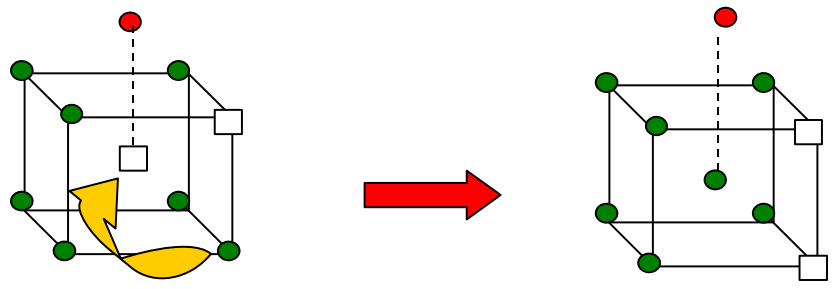
pair of  $V_A$  and  $V_B$  vacancies

Variant 1: generation of  $A_B$  and  $B_A$  antisite pairs



Result:  
 pair of  $V_A$  and  $V_B$  vacancies  
 +  
 pair of  $A_B$  and  $B_A$  antisites  
 Process may continue !

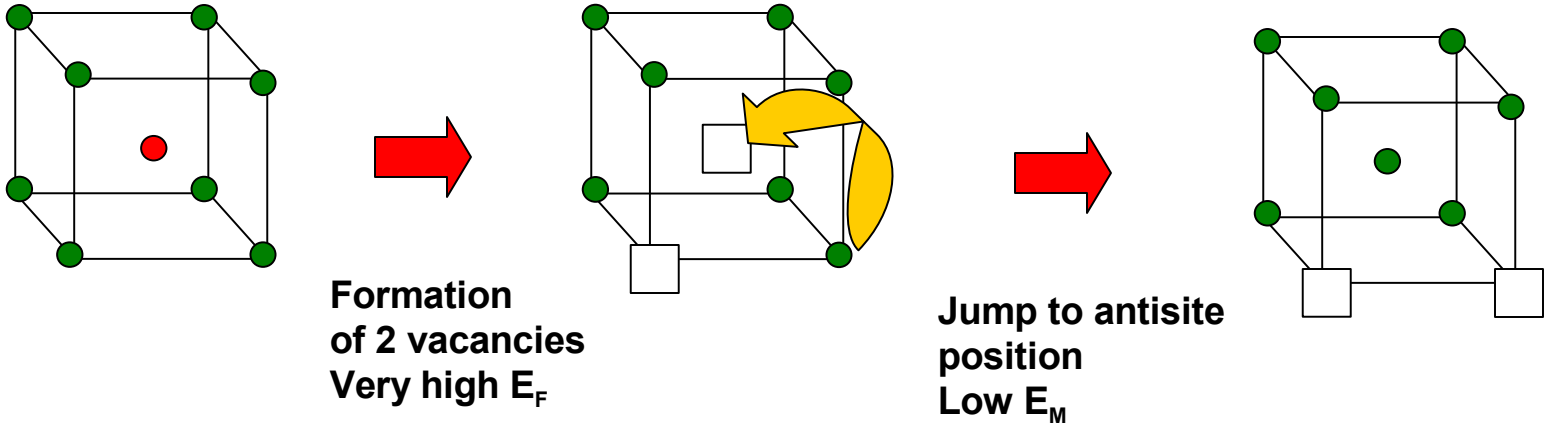
Variant 2: generation of triple defects



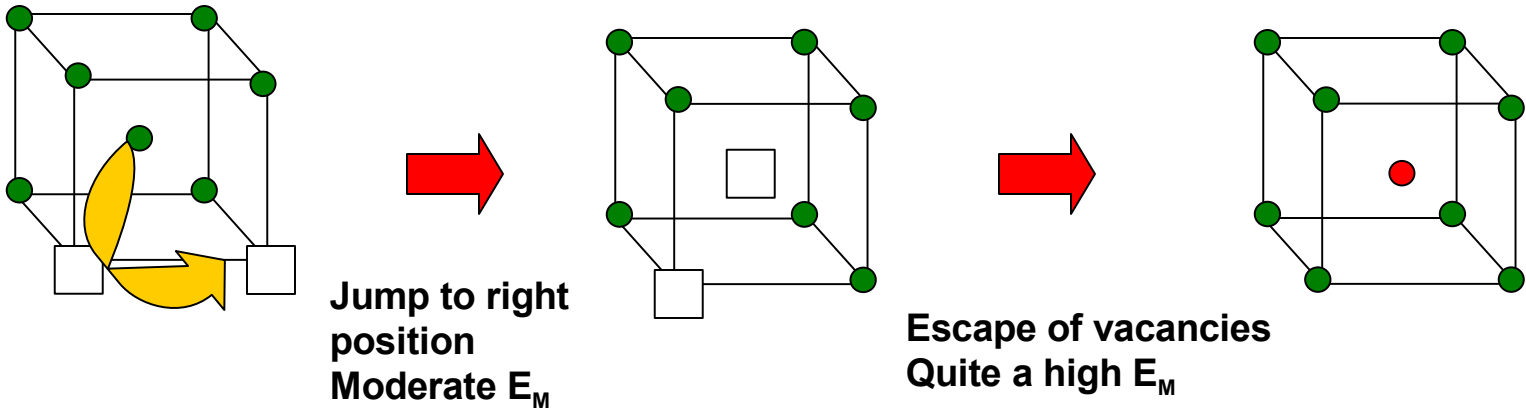
Result:  
 pair of  $V_A$  vacancies  
 +  
 single  $A_B$  antisite  
 „triple defect”  
 Vacancies almost immobile !  
 Condition:  
 $E_F(V_B) \gg E_F(A_B)$

# „ORDER-ORDER” KINETICS IN TRIPLE-DEFECT B2-ORDERED AB SYSTEMS:

## DISORDERING (GENERATION OF ANTISITE DEFECTS):



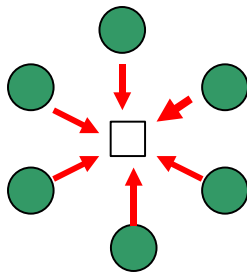
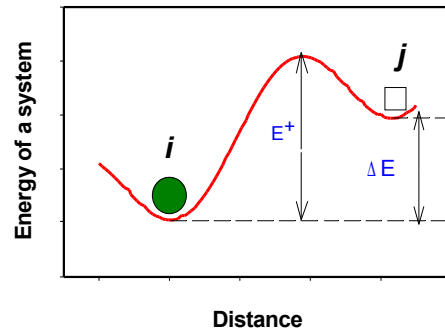
## ORDERING (ELIMINATION OF ANTISITE DEFECTS):



# STANDARD MONTE CARLO SIMULATIONS IN BULK:

- $A_3B$  or  $AB$  binary system with  $L1_2$ ,  $L1_0$  or  $B2$  superstructure,
- $40 \times 40 \times 40$  cubic cells,
- 1 vacancy (10 vacancies in a piloting study)

general assumption: vacancy mechanism of atomic migration



Glauber dynamics algorithm:

$$\Pi_{i \rightarrow j} = \frac{\exp\left[-\frac{\Delta E}{kT}\right]}{1 + \exp\left[-\frac{\Delta E}{kT}\right]}$$

„Residence-time“ algorithm:

$$\Pi_{i \rightarrow j} = \Pi_0 \times \exp\left[-\frac{E_i^+ - E_i}{kT}\right]$$

$$\Pi_0 = \left[ \sum_l \exp\left(-\frac{E_l^+ - E_l}{kT}\right) \right]^{-1}$$

# **PROBLEM:**

**Because of possible correlation between  
antisite and vacancy concentrations  
MC simulation with fixed number of  
vacancies is no longer justified**



# MODEL: EQUILIBRIUM CONCENTRATION OF THERMAL VACANCIES

W. Schapink, Scr. Metall. 3, 113, (1969).

S. H. Lim, G. E. Murch, W. A. Oates, J. Phys. Chem. Solids 53, 181, (1992)

R. Kozubski, Acta Metall. Mater. 41, 2565, (1993).

**Lattice gas:**

**A-atoms + B-atoms + vacancies**

$$C_A/C_B = \text{const},$$

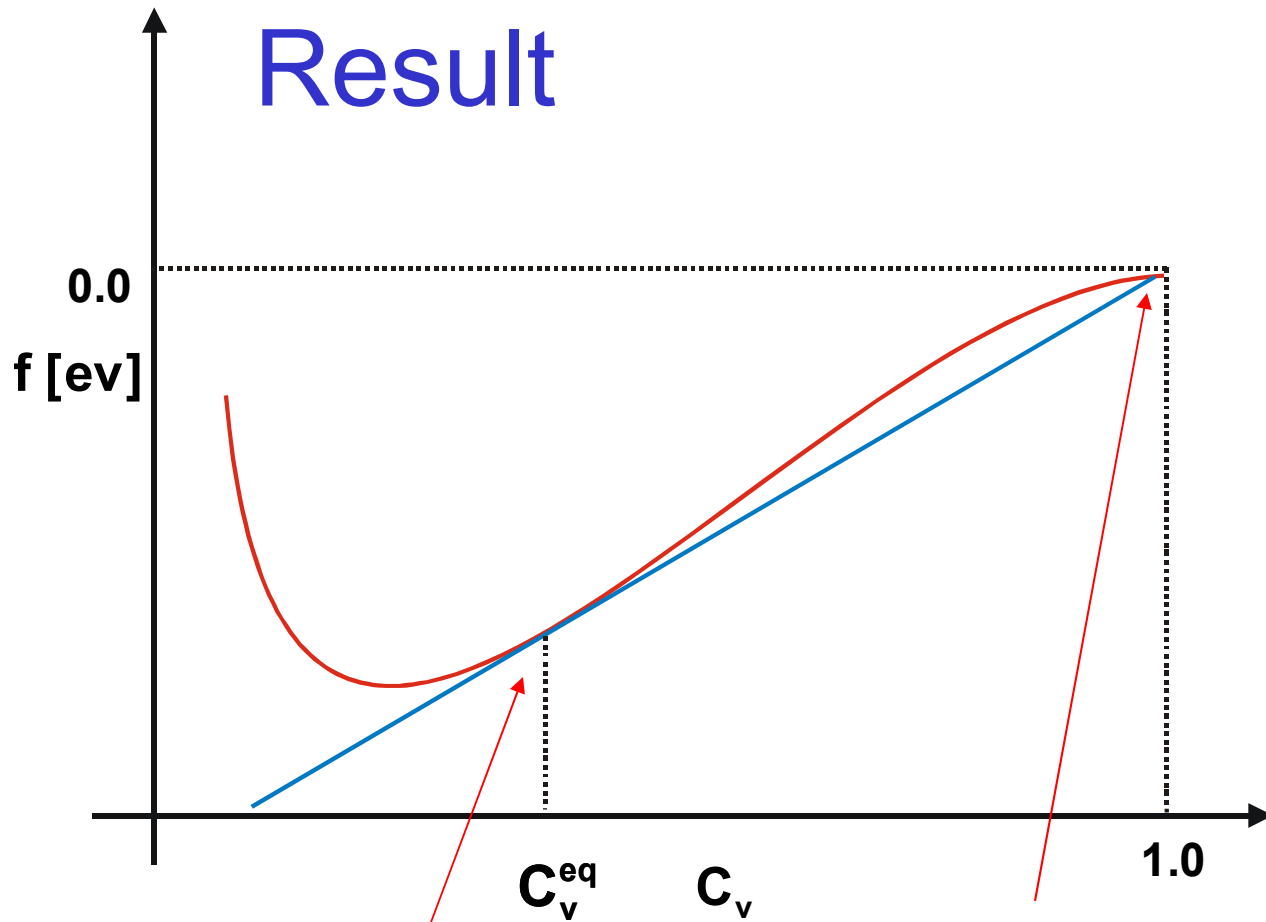
$$C_V \gg C_A, C_B$$

$$2V_{AB} - V_{AA} - V_{BB} < 0 \text{ (tendency for B2 ordering)}$$

$$V_{VV} = 0$$



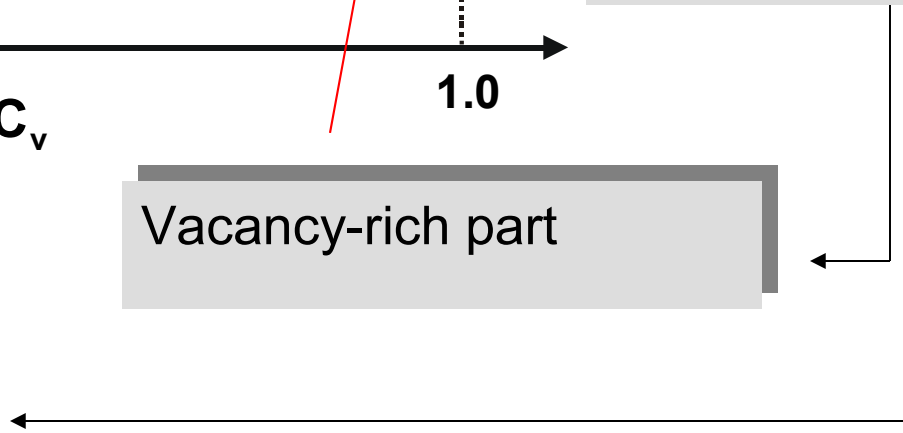
# Result

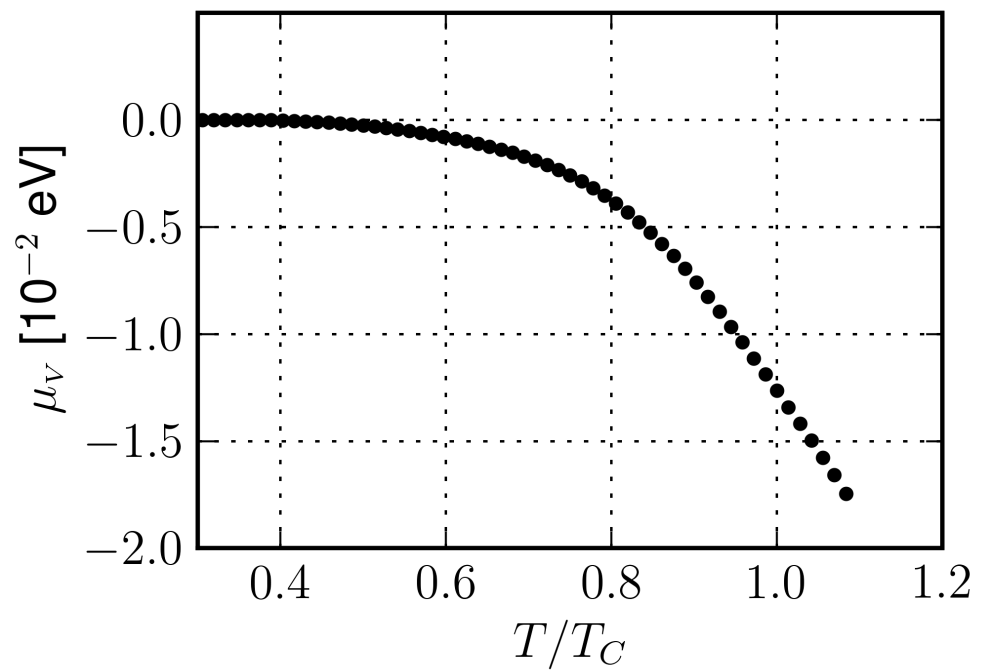
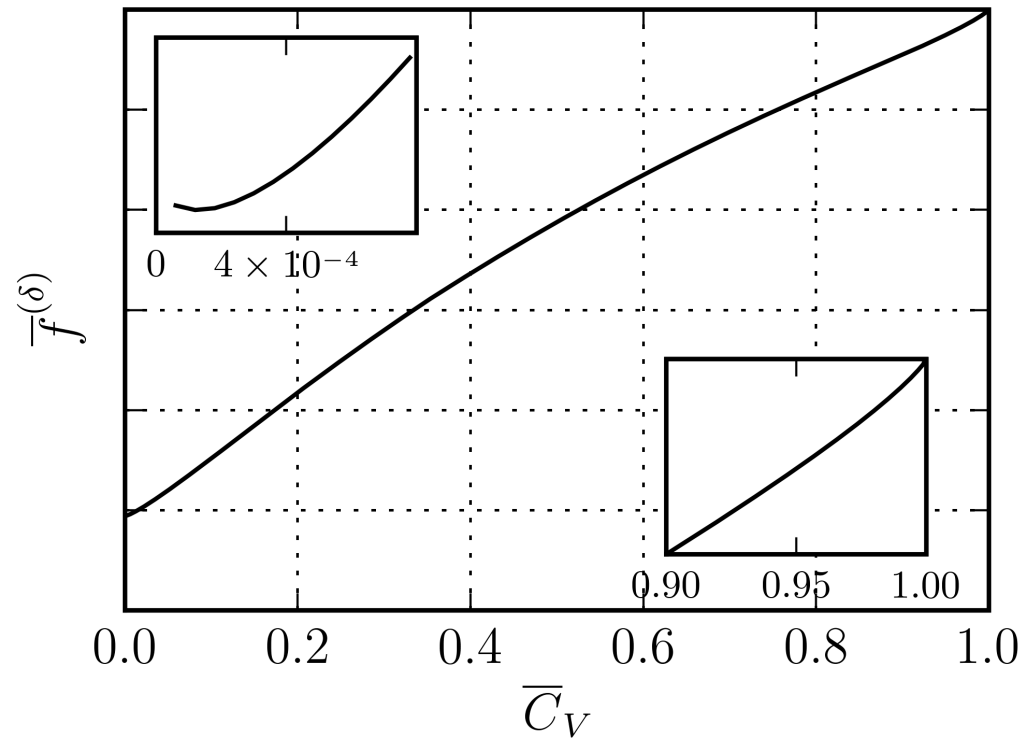


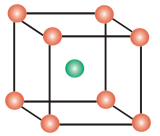
Interpretation:  
lattice gas  
decomposes into

Vacancy-poor part:  
crystal with  
equilibrium vacancy  
concentration

Vacancy-rich part







*Definitions :*

$$W = 2V_{AB} - V_{AA} - V_{BB}$$

$$E_{as} = V_{AA} - V_{BB}$$

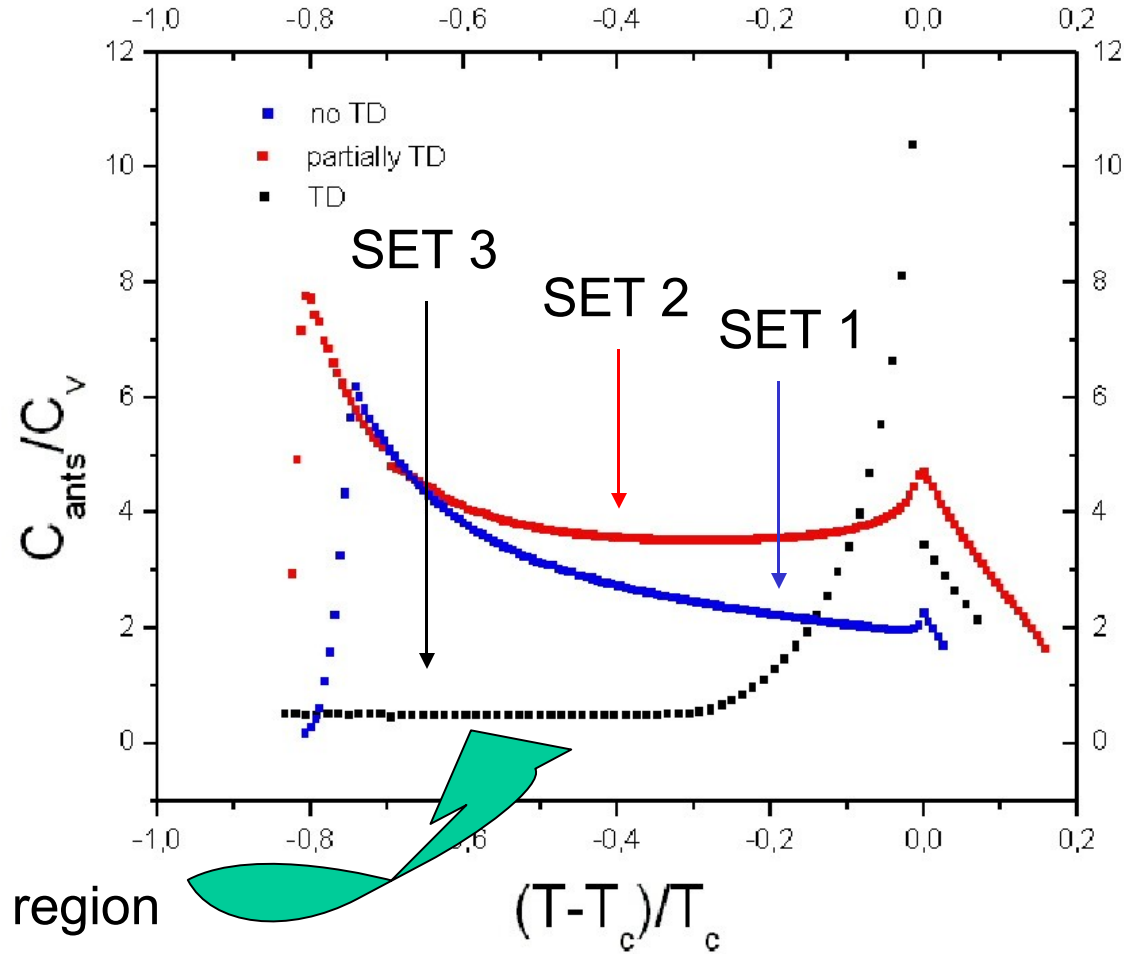
**Calculations were made for various sets of energies**

	W [eV]	$E_{as}$ [eV]	$V_{BB}$ [eV]	$V_{AV}$ [eV]	$V_{BV}$ [eV]	Structural vacancies	Plateau
SET1	-0,08	-0,03	-0,05	0,0	0,0	No	No
SET2	-0,08	-0,07	-0,05	0,0	0,0	No	Partially
SET3	-0,08	-0,07	-0,05	0,051	-0,051	Yes	Yes

# STOICHIOMETRIC BINARY SYSTEM

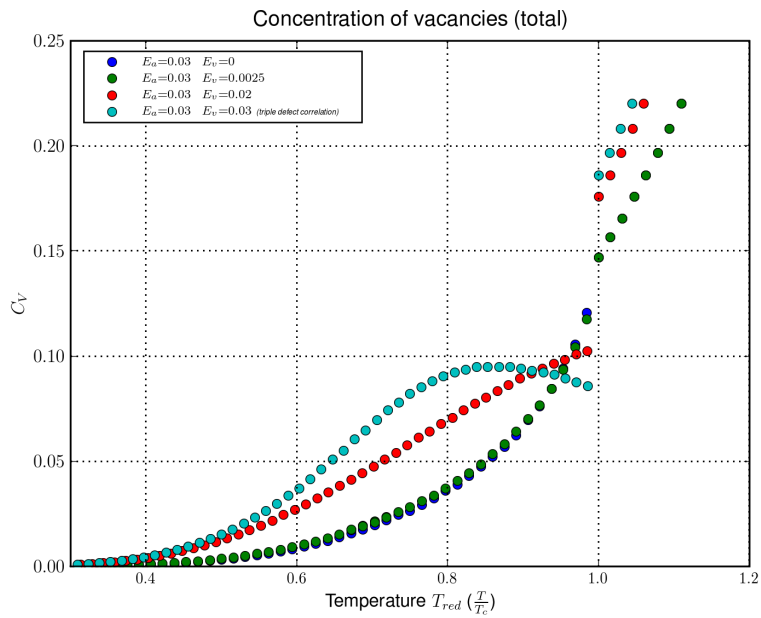
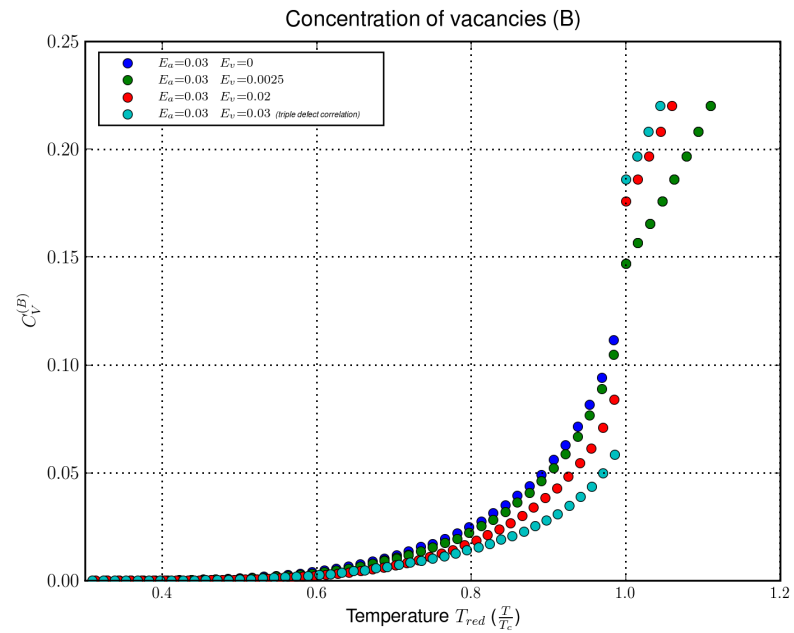
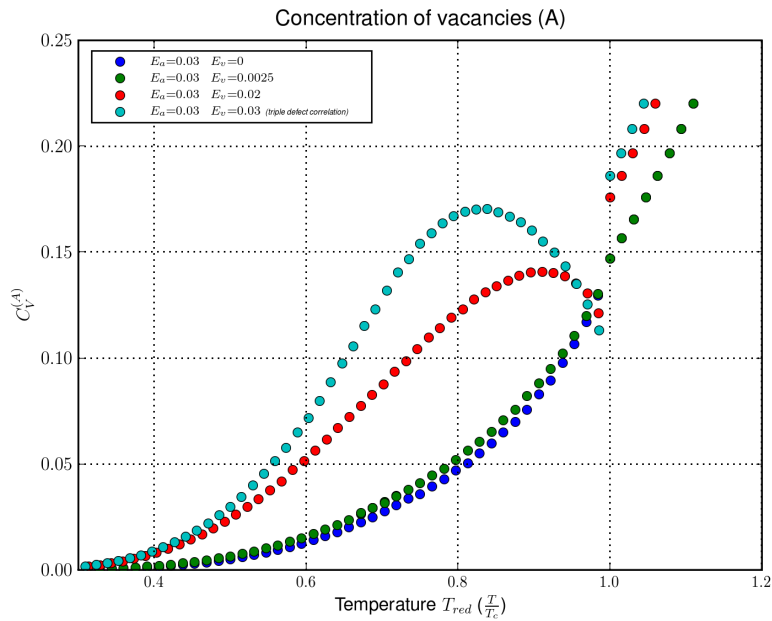


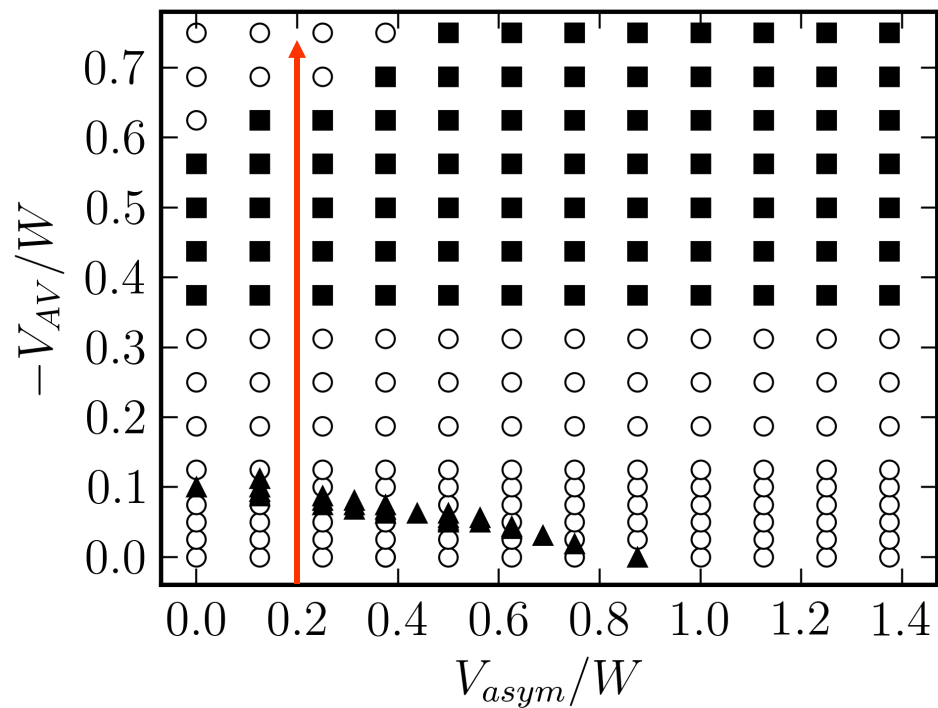
# MAIN RESULT (from Bragg-Williams calculations)



Triple Defect region

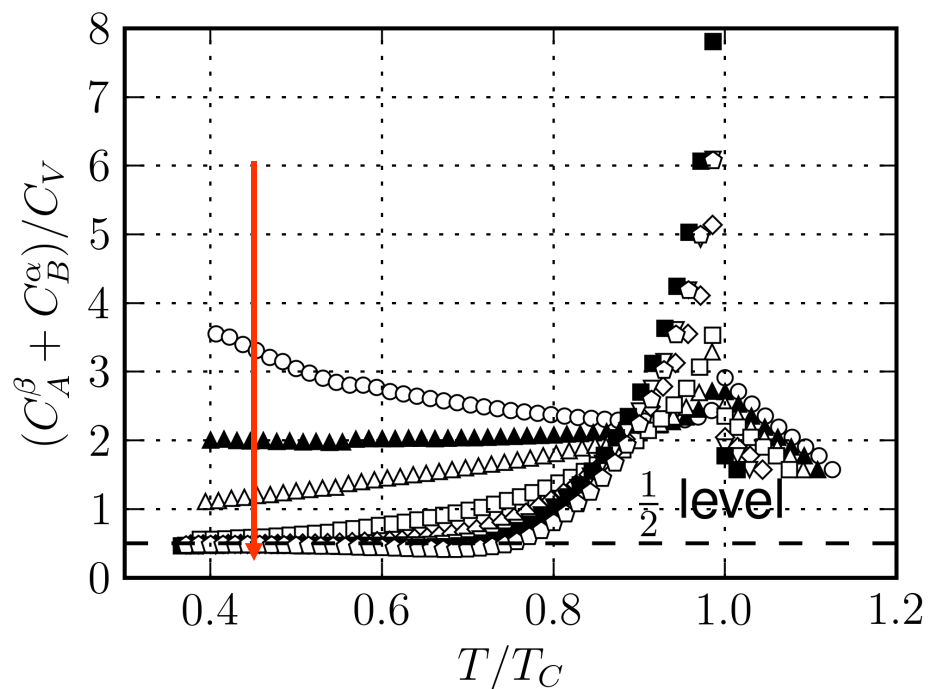
IN PROGRESS: MC on Grand Canonical Ensemble





no plateau;  $\square$  "higher-level plateau"; "plateau".

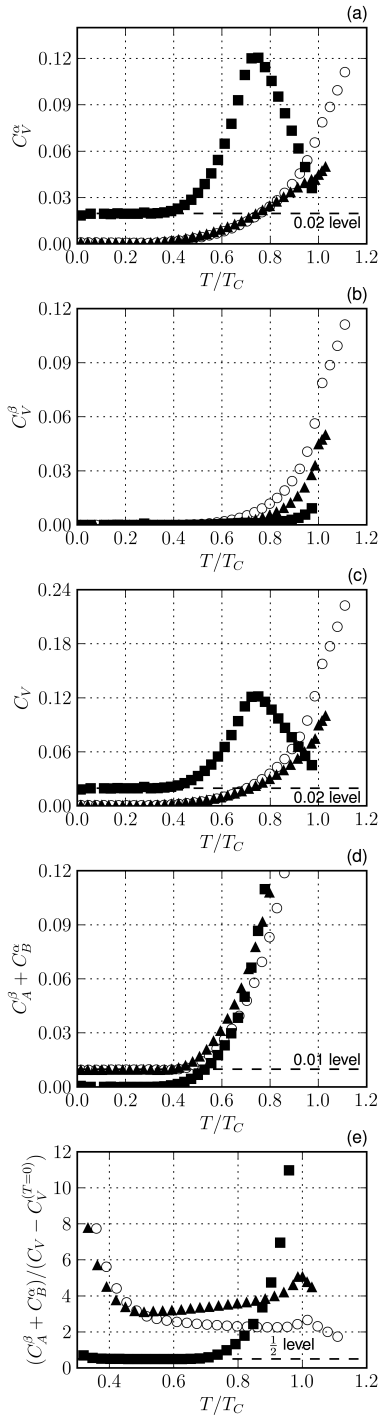
## SET 3 energetics





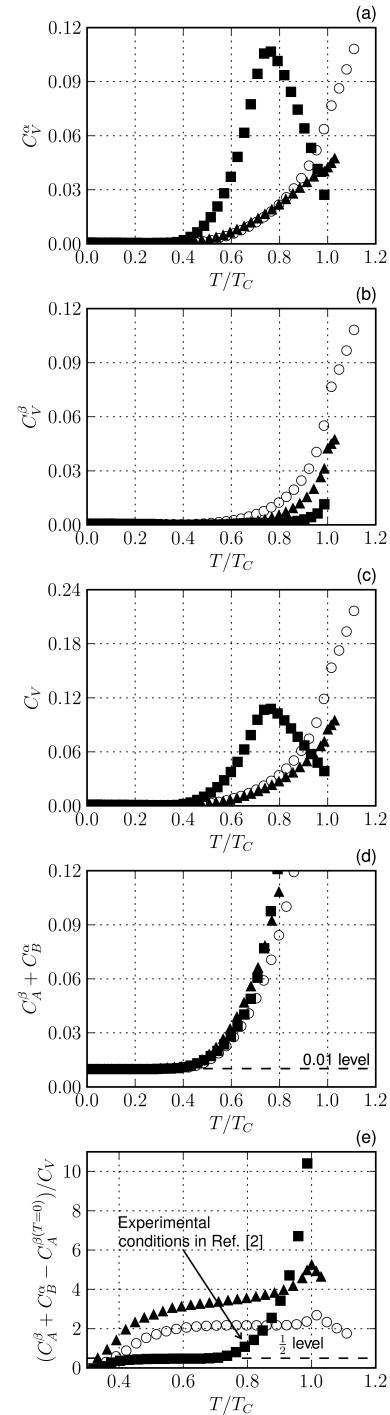
# **NON-STOICHIOMETRIC BINARY SYSTEMS**



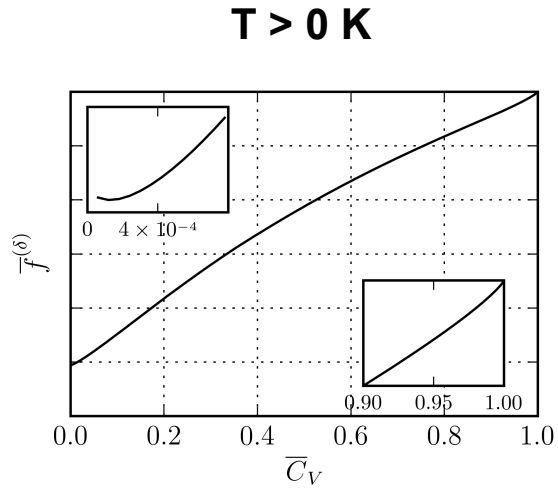
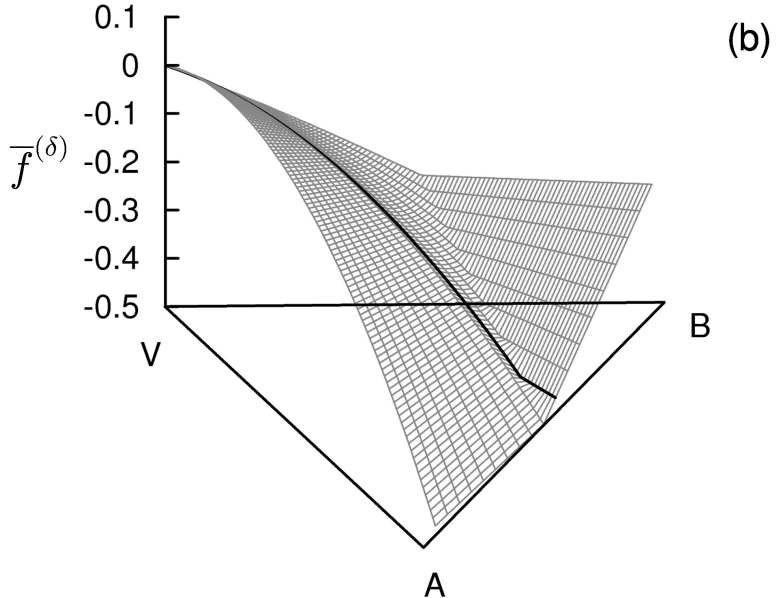
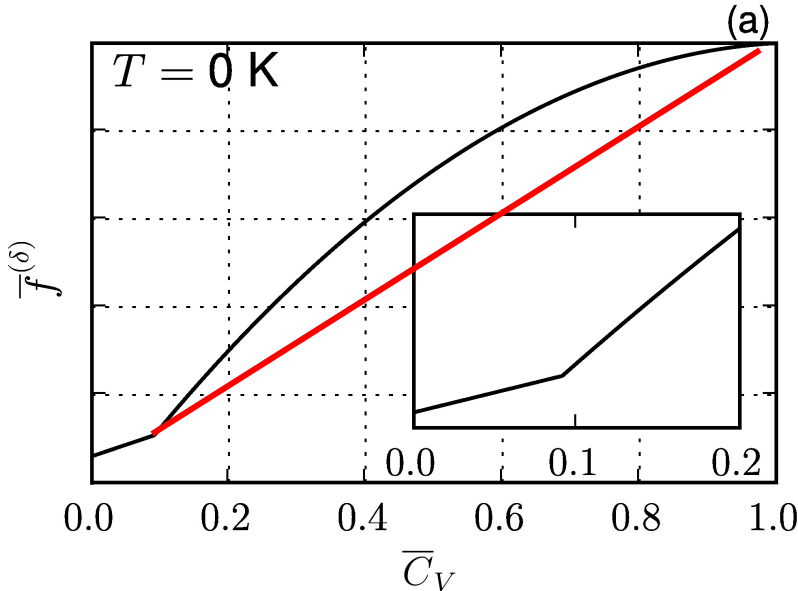


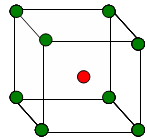
**A<sub>49</sub>B<sub>51</sub>**

**A<sub>51</sub>B<sub>49</sub>**



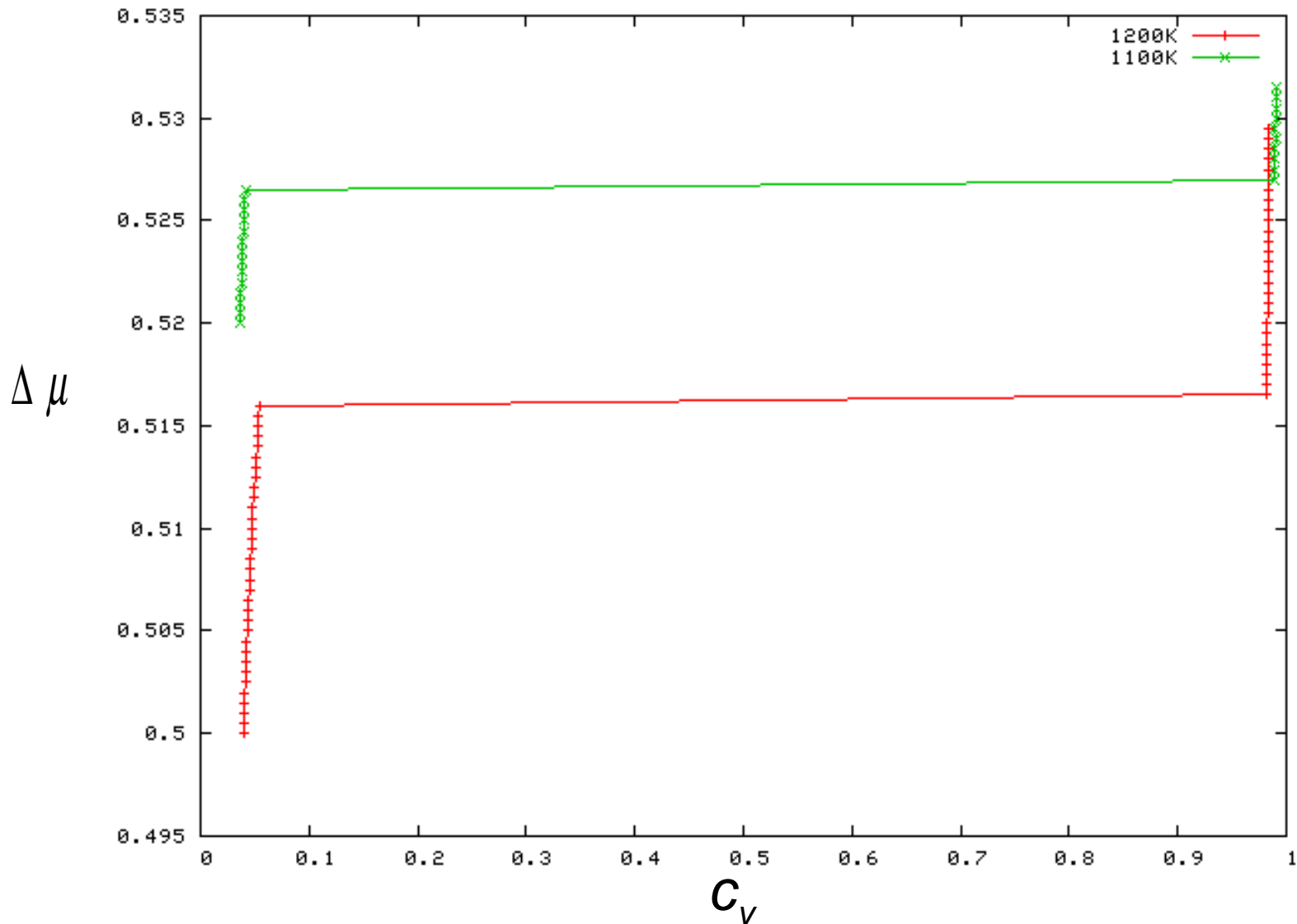
# GENERATION OF CONSTITUTIONAL VACANCIES:

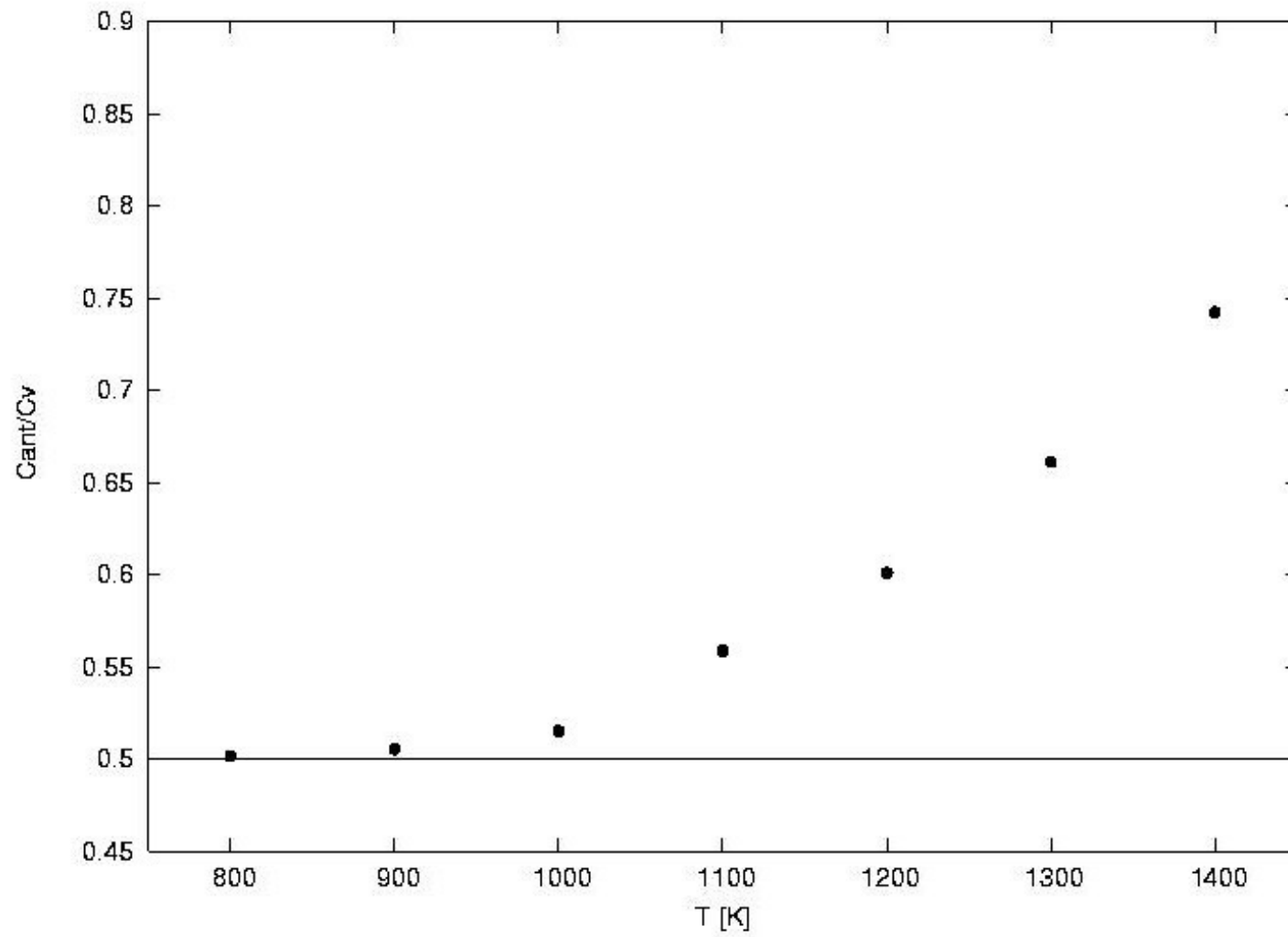




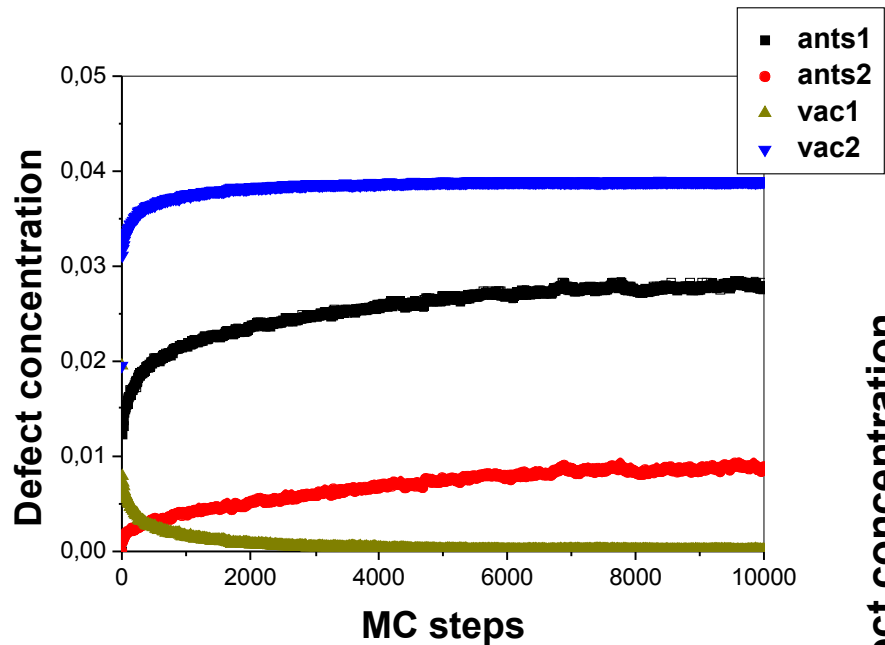
# Two phases decomposition in SGCMC

Monoatomic system with vacancies in bcc  $V_{aa}=-0.12$ [eV]  $V_{vv}=0$  [eV],  $V_{av}=V_{va}=-0.01$  [eV]

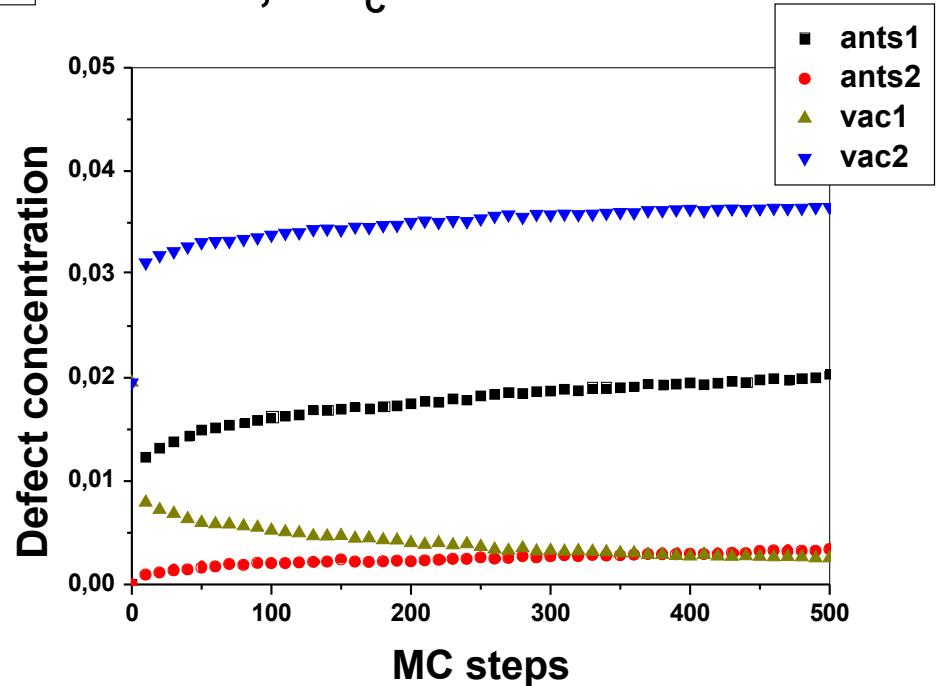




# FIRST MC SIMULATIONS OF **DISORDERING KINETICS**



**SET 3 of pair-interaction energies**  
 $T = 0,5 \times T_c$



## **Conclusions:**

Initial stage: **fast** creation of triple defects (only A-antisites)

Continuation: **very slow** generation of A- and B-antisites

# CONCLUSIONS:

- **Triple-defect-type correlation between antisite and vacancy concentrations in B2-ordering AB binary follows from a Bragg-Williams model of atom-vacancy lattice gas**
- **Vacancy trapping by triple defects results in substantial slowing-down of „order-order” relaxations in B2 intermetallics showing very high vacancy concentration**